

**GLOBAL EXISTENCE AND DECAY PROPERTIES OF SOLUTIONS
FOR SOME STRONGLY DAMPED NONLINEAR WAVE EQUATIONS**

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ABSTRACT. In this paper we shall investigate the decay properties of solutions of p -Laplacian wave equation with strong damping. For this end we use the multiplier method combined with some integral inequalities due to Komornik.

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