

## ON THE QUATERNION PADOVAN NUMBERS

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ABSTRACT. In this paper, we define the quaternion Padovan sequence. We obtain some identities for this quaternion sequence. Also, we derive a plastic-like ratio.

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