

THE GENERALIZED ISI INDEX OF SOME DERIVED NETWORKS

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ABSTRACT. A network is formed by nodes communicating with each other. A topological index is a numerical quantity which is obtained from a network or a graph of a chemical compound, which characterizes the molecule on the basis of its structural properties. Recently Buragohain *et al.* [8] propose and study a novel generalized topological index, which is termed as generalized ISI index for some chemical structures. In this communication, we compute this generalized topological index for some derived networks, namely Honeycomb network, Sierpinski network, Cayley tree network, Butterfly network, Benes network and Mesh-derived networks.

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