

**ON PEAK POINTS AND MONOTONICITY OF DOUBLE SEQUENCES  
BY SOME SUBMETHODS**

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ABSTRACT. In this paper, we defined the notion of peak points of real valued double sequences and gave several theorems on this subject. Also, we obtained some important inclusion results about  $A$ -statistical monotonicity for double sequences with double Cesàro submethod and double deferred Cesàro mean.

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