

**ON q -QUASI CONVEXITY RELATED
WITH STRONGLY JANOWSKI FUNCTIONS**

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ABSTRACT. Using generalized Janowski functions and q -calculus, the class $C_q^*[A, B, \gamma]$ is defined and its properties are studied which include coefficient bounds and Bernardi operator. Some known and new interesting results are pointed out as applications of the main results.

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Received: October 04, 2020. Revised: January 13, 2021.

2010 Mathematics Subject Classification: 30C45, 30C50.

Key words and phrases: q -derivatives, q -quasi convexity, convolution operator, starlike functions, close-to-convex functions.

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