

PROJECTED DYNAMICAL SYSTEM FOR VARIATIONAL INEQUALITIES

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ABSTRACT. In this paper, we suggest and analyze a new projected dynamical system for variational inequalities using the technique of Wiener-Hopf equations. We study the globally asymptotic stability of the solution of the projected dynamical system for the pseudomonotone operators.

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