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A SINGULAR FRACTIONAL DIFFERENTIAL EQUATION WITH RIEMANN-LIOUVILLE INTEGRAL BOUNDARY CONDITION

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Abstract. We investigate the existence of positive solutions for a singular fractional differential equation with a integral boundary condition.

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