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A COMPANION OF OSTROWSKI TYPE INEQUALITIES FOR FUNCTIONS OF TWO VARIABLES WITH BOUNDED VARIATION

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Abstract. In this paper, a companion of Ostrowski type inequalities for functions of two independent variables with bounded variation is obtained and some sharp inequalities are proved. Application to quadrature rule is also provided.

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