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COMPLETE SUBMANIFOLDS OF SPACE FORMS AND APPLICATION OF BOCHNER FORMULA

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Abstract. The present paper deals with the classification of a complete submanifold of a Riemannian space form and also a complete CR-submanifold of a complex space form by applying Bochner formula.

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