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ON CONVERGENCE THEOREMS OF MODIFIED S-ITERATION PROCESS FOR GENERALIZED ASYMPTOTICALLY QUASI-NONEXPANSIVE NON-SELF MAPPINGS

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Abstract. In this paper, we establish some strong and weak convergence results of modified S-iteration process for two generalized asymptotically quasi-nonexpansive non-self mappings in the framework of Banach spaces. Our results extend and generalize the previous works from the current existing literature.

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