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SOME FIXED POINT RESULTS FOR MULTI-VALUED CONTRACTIVE MAPPINGS IN PARTIAL b-METRIC SPACES

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Abstract. In this paper, we prove some fixed point results in partial b-metric spaces. We derive some consequences and corollaries from our obtained results. Our results improve many recent fixed points results and generalize some classical known results in the literature.

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