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SUZUKI TYPE UNIQUE COMMON FIXED POINT THEOREM FOR FOUR MAPS USING α-ADMISSIBLE FUNCTIONS IN ORDERED PARTIAL METRIC SPACES

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Abstract. In this paper, we obtain a Suzuki type unique common fixed point theorem for four self maps satisfying (ψ, ϕ, φ)-contractive condition using α-admissible function in ordered partial metric spaces. Also we give an example to illustrate our main theorem.

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